Integrated Controls-Structures Design Methodology: Redesign of an Evolutionary Test Structure

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An optimization-based integrated controls-structures design methodology for a class of flexible space structures is described, and the phase-0 controls-structures-integration evolutionary model, a laboratory testbed at NASA Langley, is redesigned using this integrated design methodology. The integrated controls-structures design is posed as a nonlinear programming problem to minimize the control effort required to maintain a specified line-of-sight pointing performance, under persistent white noise disturbance. Static and dynamic dissipative control strategies are employed for feedback control, and parameters of these controllers are considered as the control design variables. Sizes of strut elements in various sections of the controls-structures-integration evolutionary model are used as the structural design variables. Design guides for the struts are developed and employed in the integrated design process to ensure that the redesigned structure can be effectively fabricated. The superiority of the integrated design methodology over the conventional design approach is demonstrated analytically by observing a significant reduction in the average control power needed to maintain specified pointing performance with the integrated design approach.

Introduction

¶ URRENTLY spacecraft are designed in separate iterative sequences within the structural and control disciplines. The structural design, performed first, takes into account loading considerations that would occur during launch, reboost, or operational maneuvers. The sizes and masses of mission-related components are estimated, and a structure is designed that maintains the desired spatial relationships among various components during operations. In the next stage, a controller is designed for the fixed structure to orient, guide, and move the spacecraft to obtain the required spacecraft performance. Measures of spacecraft performance may take different forms, such as limits on pointing jitter, transient response deviations, control power requirements, and so on. The control design must also provide satisfactory closed-loop stability robustness. This separate-discipline approach has been used successfully in most of the missions in the past. It works well when a relatively high-stiffness structure is feasible, the nonstructural components are concentrated masses and inertias, and the performance requirements of the missions are not stringent. In these cases the structural modes are beyond the controlled bandwidth, so that there is minimal control-structure interaction. However, this approach will not meet the stringent performance requirements of future space structures. A number of future space missions will utilize flexible structures in low-Earth orbits and geostationary orbits. Examples of such missions include space science platforms, space processing facilities, and Earth observation systems. Such missions typically require distributed-mass components, such as booms, solar arrays, and antennas, whose dimensions range from a few meters to possibly hundreds of meters. To minimize the costs of construction, launching, and operations, it is necessary to make the structure as light as possible. The combination of large size and low structural mass, however, leads to increased flexibility and makes attitude control of the structure to a specified precision more difficult.

Controls-structures interaction (CSI) in the form of destabilizing spillover^{1,2} has been verified in simple Earth-based laboratory experiments, as well as in the design, analysis, ground development, test, and flight operation of space systems in industry. The current approach to solving CSI problems is to design the spacecraft to avoid undesired dynamical interaction. This generally requires either stiffening the structure or slowing down the control system response. Stiffening the structure simplifies the control design problem in that the predominant dynamics tend toward rigid body, but is costly in terms of mass as well as launch packaging, leading to increased fuel consumption. Slowing down the control response produces control inputs that have less of a chance of producing destabilizing effects, but is costly in terms of reduced performance capability. Neither approach is completely satisfactory. A new design approach is needed that has the capability of avoiding any damaging aspects of CSI, while at the same time identifying and exploiting the beneficial aspects.

A number of studies have been presented in the past decade using integrated controls-structures design methodologies to enhance the overall performance of the controlled system. Minimization of structural mass, subject to constraints on closed-loop eigenvalues, damping parameters, and structural natural frequencies, has been considered in Refs. 3 and 4. Although dependence of control cost on the structural parameters is clear, since system matrices are functions of structural parameters, total structural mass is not considered directly as a function of control parameters, or control effort, in these studies. The effect of variable actuator masses, as a function of control effort, is addressed in Refs. 5 and 6. Other studies^{4,7} have considered minimization of a control objective, such as the norm of feedback gain matrices, as a measure of control effort, with constraints on closed-loop response and total structural mass. A covariance approach is used in Ref. 8 to constrain overall system response with bounds on the allowable control energy. Multiobjective optimization has been used to optimize a combination of structural objectives, such as structural mass, and control objectives, such as control energy or quadratic objective functions obtained from linear regulator theory. 9-11 Multiobjective optimization provides tradeoffs between competing objectives, thus providing a continuum of system designs, with different performance characteristics. Reference 12 includes a good survey of numerous other approaches employed for integrated controls-structures design. Most of the techniques in the

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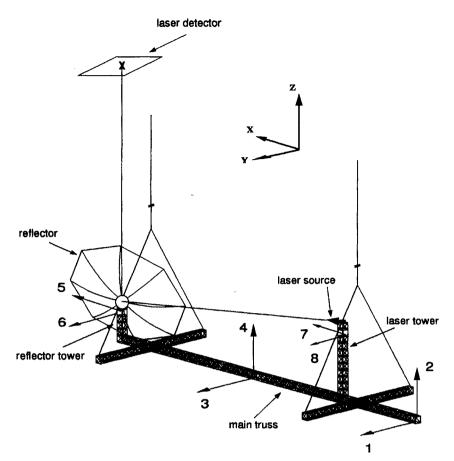


Fig. 1 Schematic of the CEM testbed.

literature, however, have been applied to simple analytical models or laboratory apparatuses. Only recently have there been some studies in integrated design of large-order flexible space structures (with thousands of degrees of freedom). ^{5,6,13,14}

The CSI program at NASA Langley¹⁵ has been developing an integrated controls-structures design methodology that is described in this paper. The design methodology is based on the recognition that a high degree of coupling exists between the control and structural disciplines in the control of flexible space structures. Rather than performing separate structural and control designs, a unified environment for integrated control-structural modeling, analysis, and synthesis is developed. Within this environment, a design iteration consists of updating all critical (control and structure) design variables in a single integrated computational framework by assessing controlled performance with the current design variables. Parameter optimization techniques, employing nonlinear mathematical programming, are used for the synthesis of an optimal integrated structure. Realistic constraints, which have not been considered in previous literature, were imposed on the current design process to ensure that the structure obtained through integrated design could be practically fabricated. For example, the strut designs were obtained using design curves relating effective areas and effective densities that imposed the requirements of manufacturability on the design process. This structure was subsequently used to verify the benefits of controlsstructures integrated design experimentally, as described in Ref. 16.

The phase-0 CSI evolutionary model (CEM), a laboratory test structure at NASA Langley (shown in Fig. 1), was used as the candidate flexible structure for controls-structures integrated redesign. Two dissipative control strategies, namely, static dissipative and dynamic dissipative controllers, were employed for feedback compensation, since these compensators guarantee closed-loop stability in the presence of unmodeled dynamics and parametric uncertainties.¹⁷ The performance measure for optimization is the average control energy required to maintain a prescribed line-of-sight pointing, in response to persistent, white noise at specified disturbance locations. Integrated redesign of the phase-0 CEM was performed with the two control strategies to improve the performance of the

controlled system. Concurrent with the integrated design process, control-optimized dissipative controllers were designed for the nominal phase-0 CEM. A comparison of the controlled performance of the integrated designs with that of the conventional control-optimized designs indicate over 40% reduction in control power, while providing the same pointing performance. These results clearly demonstrate the advantage of integrated controls-structures design methodology over the traditional sequential approach. The redesigned structure was fabricated and assembled in the laboratory, and a number of active control experiments were performed with it to experimentally validate these results. This effort represents the first experimental validation of the integrated design methodology for realistic flexible space structures and is described in Ref. 16.

Mathematical Models

Structural Model

The dynamics of flexible space structures can be treated as dynamics of a distributed parameter system from a continuum mechanics viewpoint. Applying the principles of classical mechanics to the distributed parameter system results in a system of partial differential equations with associated initial and boundary conditions. This framework for description of structural dynamics, however, is of limited value in characterizing the dynamics of realistic, flexible space structures. Space structures are conventionally analyzed using approximate techniques, such as the finite element method. A finite dimensional, linear, and time-invariant mathematical model of a flexible space structure is given as

$$M\ddot{x} + D\dot{x} + Kx = \tilde{B}u + \tilde{H}w \tag{1}$$

where x is an $n \times 1$ displacement vector; u is the $m \times 1$ control input vector, w is the $p \times 1$ disturbance vector, M is the positive definite inertia matrix, D is the positive semidefinite open-loop damping matrix, K is the positive semidefinite stiffness matrix, \tilde{B} is an $n \times m$ control influence matrix, and \tilde{H} is $n \times p$ disturbance influence matrix. The rate and performance output equations are

$$\mathbf{y}_r = \tilde{C}_r \dot{\mathbf{x}}; \qquad \mathbf{y}_{per} = \tilde{C}_{per} \mathbf{x}$$
 (2)

where y_r is the rate measurement, y_{per} is a performance vector, and C_r and C_{per} are the rate output and performance output influence matrices, respectively. The second-order representation of the structure given in Eq. (1) is obtained by finite element modeling of the structure (the order of these models can be quite large). For design and analysis purposes, the order of the system is reduced using a modal truncation approach, wherein significant modes in the inputoutput characterization of the plant are retained and the remaining modes are truncated. The system equations in modal coordinates for the retained modes are written as

$$M_r \ddot{q}_r + D_r \dot{q}_r + K_r q_r = \Phi^T \tilde{B} u + \Phi^T \tilde{H} w \equiv \Gamma_c^T u + \Gamma_d^T w$$
 (3)

where q_r is an $r \times 1$ vector of modal amplitudes; M_r , D_r , and K_r are the generalized inertia, damping, and stiffness matrices, respectively; and Φ is an $n \times r$ matrix whose columns are the r structural eigenvectors associated with the included modes. If the mode shapes are normalized with respect to the inertia matrix and modal damping is assumed, then $M_r = I_{r \times r}$, $D_r = \text{diag}\{2\zeta_1\omega_1, \ldots, 2\zeta_r\omega_r\}$, and $K_r = \text{diag}\{\omega_1^2, \ldots, \omega_r^2\}$, where ω_i and ζ_i , $i = 1, \ldots, r$, are the open-loop frequencies and damping ratios. With collocated and compatible measurement sensors and control actuators,

$$\mathbf{y}_r = \tilde{\mathbf{B}}^T \Phi \dot{\mathbf{q}}_r = \Gamma_c \dot{\mathbf{q}}_r \tag{4}$$

Note that the collocation of these sensors and actuators is necessary for the implementation of the dissipative controllers. This collocation guarantees the system to be minimum phase, i.e., transmission zeros and poles of the system are in the left-half plane, and enhances the stability robustness of the overall system.²

the stability robustness of the overall system.² Defining the state vector, $\mathbf{z} = \{\mathbf{q}_r^T \mid \dot{\mathbf{q}}_r^T\}^T$, the dynamics of the system can be written in a first-order form:

$$\dot{z} = Az + Bu + Hw \tag{5}$$

where

$$A = \begin{bmatrix} 0 & I_{r \times r} \\ -K_r & -D_r \end{bmatrix}; \qquad B = \begin{bmatrix} 0 \\ \Gamma_c^T \end{bmatrix}; \qquad H = \begin{bmatrix} 0 \\ \Gamma_d^T \end{bmatrix}$$

The rate output and performance output vectors are given by

$$y_r = [0 \quad \Gamma_c]z \equiv C_r z; \qquad y_{per} = [\tilde{C}_{per}\Phi \quad 0]z \equiv C_{per}z$$

Here, $C_{\rm per}$ is the output influence matrix associated with the performance output $y_{\rm per}$.

Controller Design Methods

Control system design for flexible space structures is a challenging problem because of their special dynamic characteristics that include a large number of structural modes within the controller bandwidth; low, closely spaced structural frequencies; very small inherent damping; and a lack of accurate knowledge of modal parameters. Moreover, the controller must be of a reasonably low order to the implementable and must also satisfy the performance specifications (i.e., constraints on root-mean-square (rms) pointing error, or the desired closed-loop bandwidth). The controller must also have robustness to nonparametric uncertainties, such as unmodeled structural modes, and to parametric uncertainties, that is, errors in the knowledge of the design model.

Two major categories of controller design methods for flexible space structures are model-based controllers and dissipative controllers. A model-based controller generally consists of a state estimator (a Kalman–Bucy filter, or some other observer) followed by a state feedback controller. The state estimator utilizes the knowledge of the design model in its prediction part. Using multivariable frequency-domain design methods, such controllers can be made robust to unmodeled structural dynamics, for example, the spillover effect can be overcome. Model-based controllers, however, generally tend to be very sensitive to uncertainties in the design model, in particular, to uncertainty in the structural modal frequencies. An analytical explanation of this instability mechanism may be found in Ref. 17.

Dissipative controllers utilize special passivity properties of structural dynamics, with collocated and compatible actuators and sensors, and provide robust stability in the presence of both nonparametric and parametric uncertainties.^{2,17} Therefore, dissipative controllers have been used for feedback control in the integrated design methodology.

Static Dissipative Controller

The simplest dissipative controller is the static or constant-gain dissipative controller. Using collocated and compatible actuators and sensors, such as torquers with attitude and attitude rate sensors and thrusters with linear position and velocity sensors, the constant-gain dissipative control law is given by

$$\boldsymbol{u} = -G_r \boldsymbol{y}_r - G_p \boldsymbol{y}_p \tag{6}$$

where y_r and y_p are $m \times 1$ rate and position measurement vectors, where m is the number of sensors; G_r and G_p are $m \times m$ symmetric, positive semidefinite rate and position gain matrices, respectively. This control law has been proven to give guaranteed closed-loop stability despite unmodeled elastic modes, parameter errors, certain types of actuator and sensor nonlinearities (such as saturation and dead zone), as long as actuator dynamics are limited to zero-order or first-order forms.² For space structures with zero frequency, rigidbody modes, position feedback is essential to ensure stability of the closed-loop system. For the ground-based structure considered in this paper, however, with nonzero frequency suspension modes, rate feedback alone is sufficient to guarantee stability. Therefore, for the integrated design and experimental studies, only rate feedback is considered. The drawback of this controller is that the achievable performance is inherently limited because of its simple mathematical structure.

Dynamic Dissipative Controller

To obtain higher performance while still retaining the highly desirable robust stability, dynamic dissipative compensators can be used. An n_c -order, two-level, dynamic dissipative controller is given by

$$\dot{\mathbf{x}}_c = A_c \, \mathbf{x}_x + B_c \, \mathbf{y}_r \tag{7}$$

$$\boldsymbol{u} = -C_c \boldsymbol{x}_c - G_r \boldsymbol{y}_r - G_p \boldsymbol{y}_p \tag{8}$$

where A_c , B_c , and C_c are the compensator system, input, and output matrices, respectively. G_r and G_p are symmetric, positive semidefinite rate and position gain matrices corresponding to the static dissipative inner loop. For ground test articles, with no zero frequency rigid-body modes, position feedback is not necessary. The dynamic compensator, in the outer loop, is dissipative if its transfer function is strictly positive real. The positive realness lemma, or the Kalman–Yacubovich lemma, 18 assures this condition when A_c is Hurwitz, (A_c, B_c) is controllable, (A_c, C_c) is observable, and there exists a matrix $P = P^T > 0$ such that

$$A_c^T P + P A_c = -Q (9)$$

$$C_c = B_c^T P \tag{10}$$

is satisfied, where $Q=Q^T\geq 0$. The main characteristic of dissipative controllers is that they do not rely on the knowledge of the design model to ensure stability. However, these controllers use this knowledge to obtain the best possible performance. This controller assures robust asymptotic stability regardless of unmodeled structural dynamics or parametric uncertainties.¹⁷

Integrated Design of the CEM

This section presents the integrated design methodology, and its application to the redesign of the nominal phase-0 CEM.

The phase-0 CEM, shown in Fig. 1, is a laboratory testbed at NASA Langley for experiments in control of flexible space structures. It consists of a 62-bay main truss (each bay is 10 in. long), two vertical towers, and two horizontal booms. The structure is suspended from the ceiling about 840 in. above the main truss using

two cables attached to the horizontal booms, as shown in Fig. 1. A laser source is mounted at the top of the taller tower, referred to as the laser tower, and a reflector with a mirrored surface is mounted on the other tower, called the reflector tower. A laser beam is reflected by the mirrored surface onto a detector surface 660 in. above the reflector. The line-of-sight pointing problem is to maintain the laser close to its nominal position on the detector surface, despite persistent disturbances. Eight proportional bidirectional air thrusters, with maximum output force of 4.4 lbs each, are available at stations 1–8, shown in Fig. 1. Almost collocated with the thrusters at the eight stations are servoaccelerometers to provide output measurements. Accelerometer signals are subsequently integrated with the aid of washout filters to provide the required rate information. A detailed description of the phase-0 CEM is available in Ref. 19.

The phase-0 CEM is representative of flexible space structures in that a number of low-frequency closely spaced modes are within the bandwidth of its controllers, inherent damping is low, and its modal parameters are uncertain. However, one major difference between any ground-based structure, which must be suspended under the influence of gravity, and space structures is the absence of zerofrequency rigid-body modes in ground-based structures. The finite element model of the system has 3216 degrees of freedom; therefore, a large computational effort is required for solution of the structural eigenvalue problem of that size. The control design model consisted of the first 30 modes of the structure that includes 24 flexible modes and 6 suspension modes (nonzero frequency, rigid-body modes, because of suspension of the structure in the presence of gravity). A modal damping ratio of 0.1% was assumed. The modal frequencies (in hertz) of the first 10 modes of the nominal phase-0 CEM are {0.147, 0.149, 0.155, 0.730, 0.748, 0.874 1.473, 1.738, 1.882, 2.294). The first 6 modes, ranging from 0.147 to 0.874 Hz, are the suspension modes. Modes 7 and 8 are the first two lateral and vertical bending modes, and mode 9 is the first torsional mode of this structure.

For the integrated design problem, white-noise disturbances of unit intensity are applied to the structure at stations 1 and 2, and the feedback control inputs are applied at stations 3-8. Experience with the phase-0 CEM structure shows that actuators at stations 7 and 8 easily destabilize the laser tower modes, in the form of spillover destabilization, which is typical in control of flexible structures. Therefore, even though actuators 7 and 8 are very efficient locations for exciting the structure, they were included for feedback control to consider the robust stability issue objectively. After actuators 7 and 8, actuators 1 and 2 are the most effective actuators in exciting the structure. Therefore, actuators 1 and 2 were chosen as disturbance sources for integrated design and experimental validation. For the design process, no sensor and actuator dynamics were included. Thus, the system dynamics are given by Eq. (5), where the matrix Γ_c contains the modal displacements at the control stations 3-8; and matrix Γ_d contains modal displacements at the disturbance stations 1 and 2. The performance vector y_{per} is the line-of-sight pointing error or deviation of the laser point on the detector system from its nominal position in local x and y coordinates. The performance output matrix \tilde{C}_{per} is computed from the kinematics of small angular motion about the nominal configuration of the system.

The feedback control configuration used for the synthesis of the integrated controls-structures design, as well as the control-optimized design, is as follows. Persistent disturbance noise w(t) is applied to the structure at the disturbance locations (stations 1 and 2), and the deviation of the line-of-sight pointing error vector $\mathbf{y}_{\text{per}}(t)$, as measured by the laser detector, is to be maintained within desired specifications. The feedback control system applies control inputs $\mathbf{u}(t)$ at control stations 3–8, using the measured outputs $\mathbf{y}_r(t)$ at nearly collocated nodes.

The design optimization problem is to minimize the steady-state average control power while maintaining a specified rms line-of-sight pointing error and without exceeding the total mass budget of the nominal phase-0 CEM. Mathematically, the design problem is to minimize

$$J = \lim_{t \to \infty} [\operatorname{tr}(E\{\boldsymbol{u}(t)\boldsymbol{u}^{T}(t)\})] \tag{11}$$

with respect to structural and control design variables, subject to the

$$\lim_{t \to \infty} \left[\operatorname{tr} \left(E \left\{ \mathbf{y}_{\text{per}}(t) \mathbf{y}_{\text{per}}^T(t) \right\} \right) \right]^{\frac{1}{2}} \le y_{\text{per}}^{\text{max}}; \qquad M_{\text{str}} \le M_{\text{max}} \quad (12)$$

where $y_{\text{per}}^{\text{max}}$ is the maximum allowable line-of-sight pointing error, M_{max} is the mass budget, tr denotes trace of the matrix, and E is the expectation operator.

For the redesign of the CEM, the limit on the rms line-of-sight pointing was chosen as y_{per}^{max} equal to 2.4 in., which is an order of magnitude reduction from the open-loop rms line-of-sight pointing for phase-0 CEM structure (which is 22.54 in.); and M_{max} was chosen to be 1.92 lb·s²/in., which is the nominal mass of phase-0 CEM structure.

Using the static or dynamic dissipative controller, the closed-loop system dynamics can be written as

$$\dot{\bar{x}} = \bar{A}\bar{x} + \bar{H}w;$$
 $y_{\text{per}} = \bar{C}_{\text{per}}\bar{x};$ $u = \bar{C}_{u}\bar{x}$ (13)

where \bar{x} is the state vector for the closed-loop dynamics, w(t) is zero mean, white noise disturbance applied at the disturbance locations, y_{per} is the line-of-sight pointing error, u(t) is the control vector, and \bar{A} , \bar{H} , \bar{C}_{per} , and \bar{C}_u are the corresponding closed-loop system matrices. The steady-state covariance matrix for the closed-loop state $\Sigma_{\bar{x}}$ is computed by solving the following Lyapunov equation²⁰:

$$\bar{A}\Sigma_{\bar{x}} + \Sigma_{\bar{x}}\bar{A}^T + \bar{H}\Sigma_w\bar{H}^T = 0 \tag{14}$$

where Σ_w is the covariance matrix for the disturbance noise w(t). The steady-state average control power is given as

$$\lim_{t \to \infty} \operatorname{tr} \{ E\{ \boldsymbol{u}(t) \boldsymbol{u}^T(t) \} \} = \operatorname{tr} \left[\bar{C}_u \, \Sigma_{\bar{x}} \bar{C}_u^T \right]$$
 (15)

and rms line-of-sight pointing error is

$$\lim_{t \to \infty} \left[\operatorname{tr} \left(E \left\{ \mathbf{y}_{\text{per}}(t) \mathbf{y}_{\text{per}}^T(t) \right\} \right) \right]^{\frac{1}{2}} = \left[\operatorname{tr} \left(\bar{C}_{\text{per}} \Sigma_{\bar{x}} \bar{C}_{\text{per}}^T \right)^{\frac{1}{2}} \right]$$
(16)

The total mass of the structure $M_{\rm str}$ is obtained from the mass matrix of the finite element analysis routines.

For the structural design, the CEM structure was divided into seven sections, shown in Fig. 2, namely, three sections in the main truss, one section for the laser tower, one section for the reflector tower, and one section each for the two horizontal booms. The primary dynamic characteristics of these sections were defined by the mass and stiffness properties of the struts and node balls comprising these sections. A typical strut and node ball of the redesigned CEM structure is shown in Fig. 3. The strut/node ball system was modeled as an axial rod between node ball centers representing the stiffness of the strut and node ball with a point mass at each end representing the mass of the node ball. The stiffness of the axial rods in each section was used as the structural design variables. From a modeling point of view the rod stiffness is defined by its effective area, length, and modulus. Given that the length and modulus of the struts were held constant, the effective area of the axial rod was used to quantify the stiffness of the struts. Therefore, three structural design variables were used in each section, namely, the effective areas of the longerons, battens, and diagonals. Thus, the integrated design of the structure involved a total of 21 structural design variables.

In an ideal design with uniform struts, the effective area of the rod would be the cross-sectional area of the strut. In this case, however, the strut is a complex member with joints and variable cross sections. What is required is a means to relate the effective area used to model the strut/node ball system to a strut that can be manufactured. The strut of Fig. 3 is composed of three sections, namely, the node ball, the tube, and the connection hardware. The system is designed such that the node ball and connection hardware remain the same for all struts. The tube portion of the strut, however, can be changed. From a stiffness point of view the strut/node ball system can be thought of as three springs in series. The end springs represent the stiffness of half a node ball and connection hardware, whereas the center spring is the stiffness of the tube. The effective area can be represented as

$$A_{\text{eff}} = \frac{(k_c K_t)\ell}{(2k_t + k_c)E_m}$$

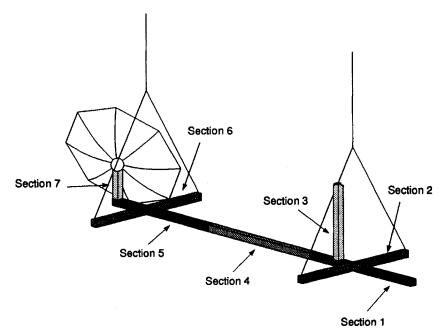


Fig. 2 CEM displaying seven sections for integrated redesign.

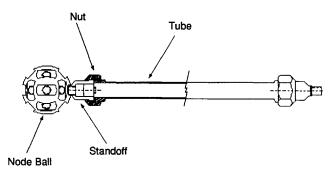


Fig. 3 Strut design for phase-1 CEM.

where k_c is the stiffness of the end springs, k_t the stiffness of the tube, ℓ the distance between node ball centers, and E_m the modulus of elasticity. If the center-to-center length, modulus, and stiffness of the node ball and connection hardware remain constant, then the effective area will be governed by the stiffness of the center tube. Associated with each effective area is an effective density defined as

$$ho_{
m eff} = rac{m}{A_{
m eff}\ell}$$

where m is the total mass of the strut, excluding the node ball mass. The effective density combined with the node ball mass is used to define the mass of the strut/node ball system in the finite element analysis of the structure.

Now the stiffness and mass properties of the structure are functions of the geometry of the center tube of the strut. To ensure that the strut/node ball system could be manufactured, design guides were semiempirically developed that defined a two-dimensional design space of manufacturable struts.²¹ The design space gives the relationship between the effective area and effective density for the strut design shown in Fig. 3. The strut design guides are shown in Fig. 4, where the dotted line corresponds to longerons and battons and the solid line is the design guide for diagonals. The curve represents the minimum mass (density) strut for a given strut stiffness (effective area). The curve is continuous because of the manufacturing process. The center tube is manufactured by turning a stock tube to a specified outer diameter, thereby allowing a variety of center tube stiffness. The design space is limited at low effective areas (toward the left end of the design guides in Fig. 4) by the strength of the strut, whereas the high effective area (toward the right end in Fig. 4) is limited by the linearity of the connection hardware. The control

design variables for static and dynamic dissipative controllers are described in the next section.

An integrated design software tool, called CSI-DESIGN, being developed at the NASA Langley, was used to perform the parameter optimizations numerically. CSI-DESIGN uses an in-core database architecture and is composed of public domain software. $^{22-24}$ The package has control, structural, and optimization modules linked together in a unified environment to perform design iterations on both structural and control design variables. A description of the contents of the CSI-DESIGN structural module may be found in Ref. 25. Employing a four-processor Alliant FX-80 digital computer, integrated optimization was performed using the Automated Design Synthesis (ADS) software.²² This design optimization took about 8 h of CPU time for each run. Gradient computations were performed using finite difference approximations. An interior penalty function method of ADS was used to solve the nonlinear programming problems. In this method, the constrained optimization problem is transformed into an unconstrained problem through creation of a pseudoobjective function that is the sum of the original objective function and an imposed penalty function (a function of the constraints²⁶). The Reverse-Cuthill-McKee algorithm²⁷ for minimizing the bandwidth of the banded stiffness and mass matrices was used to reduce computational and memory requirements. Additionally, analytical expressions for eigenvalue/eigenvector sensitivity, with respect to the structural design variables, 28 were used in the integrated design process to approximate the eigenvalues and eigenvectors at design points that are in the neighborhood of the nominal design point. This approximation was in the form of a first-order Taylor series approximation and resulted in substantial computational savings because it removes the need for costly computation of structural eigenvalues and eigenvectors at many of the optimization moves. The Lyapunov equation for closed-loop state covariance matrix, Eq. (14), is solved by transforming the matrices to a Schur form and solving the resulting linear equations, as described in Refs. 23 and 29. The control design variables used for static and dynamic dissipative control and the results of the integrated design process are described next.

Integrated Design Results

Integrated Design with Static Dissipative Controller

This section describes the control design variables for static dissipative controllers and the design optimization results. Since the test article does not have any zero-frequency rigid-body modes, only rate feedback is employed for the static dissipative controller, i.e.,

$$u = -G_r y_r \tag{17}$$

where the rate gain matrix G_r is chosen to be a 6×6 diagonal matrix, whose elements constitute six control design variables. Note that a diagonal gain matrix is used for simplicity and because the resulting decentralized controller generally exhibits superior performance robustness. The closed-loop matrices in Eq. (13) are

$$\bar{A} = \begin{bmatrix} 0 & I_{r \times r} \\ -K_r & -D_r - \Gamma_c^T G_r \Gamma_c \end{bmatrix}; \qquad \bar{H} = H$$

$$\bar{C}_{per} = C_{per}; \qquad \bar{C}_u = -[0 \quad G_r \Gamma_c]$$
(18)

Average control power and rms line-of-sight pointing error for static dissipative controllers are computed using Eqs. (15) and (16). A total of 27 design variables, 21 structural design variables, and 6 control design variables were used for the integrated design optimization with the static dissipative controller.

The results of the design optimizations are summarized in Table 1. First, the average control power was minimized with respect to the

Table 1 Results of design study with static and dynamic dissipative controllers

	rms line-of-sight error, in.	Control power, lb ²
Control-optimized design with static dissipative controller	2.4	7.11
Integrated design with static dissipative controller	2.4	4.21
Control-optimized design with dynamic dissipative controller	2.4	6.41
Integrated design with dynamic dissipative controller	2.4	3.64

control design variables while the structural design variables are fixed at the nominal phase-0 values, namely, effective areas for battons and longerons of 0.134 in.2 and effective area for diagonals of 0.124 in.² This corresponds to the conventional approach of synthesizing the best achievable controllers for a fixed structure. The control-optimized design required an average steady-state control power of 7.11 lb² to maintain rms line-of-sight error within the specified limit of 2.4 in. Next, an integrated design was performed to minimize the average control power with respect to both control and structural design variables. The results (see Table 1) indicate an average control power of 4.21 lb² to maintain the same rms lineof-sight error. The integrated design results in a reduction of more than 40% in the average control power over the conventional design for the same rms line-of-sight pointing performance. The effective areas for the structural design are shown in Table 2. Comparing the new design variables with the effective areas of the nominal phase-0 CEM, it is observed that the longerons for all three sections of the main truss, particularly the section closest to the disturbance sources, are considerably stiffened. The longerons in the laser tower are also stiffened. Conversely, the horizontal booms and the reflector tower became more flexible, partially to satisfy the mass constraint. Generally, all of the diagonals and the battens decreased in size, to satisfy a constraint on the total mass, i.e., the mass of the redesigned structure had to be less than or equal to the mass of the nominal phase-0 design. Consequently, mass was taken from the battens and diagonals and was redistributed to the longerons of some sections because longerons are quite effective in increasing the stiffness of those sections. This trend may be attributed to a tradeoff between structural controllability and observability at the actuator stations, structural observability of the performance vector, and structural excitability at the disturbance locations. The areas near the disturbance sources, i.e., stations 1 and 2, were stiffened to reduce the sensitivity

Table 2 Structural design variables for integrated design with static and dynamic dissipative controllers

Var no.	Longerons, in. ²		Var	Battens, in. ²		Var	Diagonals, in. ²		Sec.	
	Static	Dynamic	no.	Static	Dynamic	no.	Static	Dynamic	no.	Description
1	0.330	0.330	2	0.082	0.077	3	0.082	0.098	1	main truss
4	0.085	0.080	5	0.083	0.087	6	0.085	0.087	2	horizontal boom
7	0.173	0.142	8	0.082	0.086	9	0.082	0.082	3	laser tower
10	0.260	0.295	11	0.082	0.080	12	0.081	0.066	4	main truss
13	0.257	0.258	14	0.081	0.078	15	0.079	0.066	5	main truss
16	0.095	0.100	17	0.081	0.077	18	0.079	0.066	6	horizontal boom
19	0.096	0.117	20	0.081	0.083	21	0.082	0.083	7	reflector tower

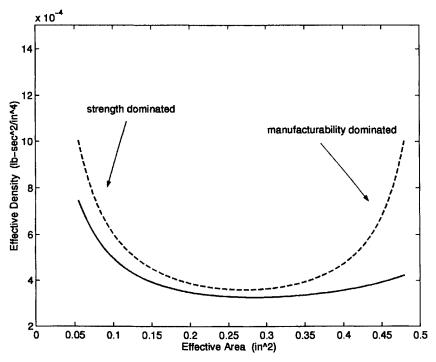


Fig. 4 Strut design curves: ----, longerons and battons and -----, diagonals.

of the structure to external disturbances at those locations, while ensuring that no appreciable loss of controllability and/or observability occurred at the control stations. The control gains for the control-optimized and the integrated designs are shown in Table 3. Generally it is observed that the gains for the redesigned system are considerably lower than those for phase-0 CEM design (except for actuator 6). This is to be expected since the required control power for redesigned system is significantly lower than that of the nominal phase-0 CEM.

Integrated Design with Dynamic Dissipative Controller

The dynamic dissipative controller represented by Eqs. (7) and (8), with no static inner loop, that is, $G_p = 0$ and $G_r = 0$, was used for the integrated redesign of the structure. The compensator state matrix A_c and compensator input influence matrix B_c , were assumed to be block diagonal, that is,

$$A_{c} = \begin{bmatrix} A_{c1} & 0 & \cdots & 0 \\ 0 & A_{c2} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & A_{c6} \end{bmatrix}$$
(19)

$$B_c = \begin{bmatrix} B_{c1} & \mathbf{0} & \cdots & \mathbf{0} \\ \mathbf{0} & B_{c1} & \cdots & \mathbf{0} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{0} & \mathbf{0} & \cdots & B_{c6} \end{bmatrix}$$
(20)

Table 3 Control design variables for integrated design, with static dissipative controllers

Var. no.	Control-optimized design	Integrated design	Actuator no.	
1	1.2110	0.5586	3	
2	2.0634	0.6837	4	
3	1.2985	0.7899	5	
4	0.5352	1.1117	6	
5	1.5050	1.0201	7	
6	0.4593	0.5982	8	

where A_{ci} and B_{ci} , i = 1, 2, ..., 6, are 2×2 matrices and 2×1 vectors, respectively, defined as

$$A_{ci} = \begin{bmatrix} 0 & 1 \\ -\alpha_i & -\beta_i \end{bmatrix}; \qquad \mathbf{B}_{ci} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$
 (21)

The parameters α_i and β_i , for $i=1,2,\ldots,6$, are the control design variables. Furthermore, the weighting matrix Q in Eq. (9) was assumed to be diagonal, that is,

$$Q = diag(q_1, q_2, \dots, q_{12})$$
 (22)

with q_j , for $j=1,2,\ldots,12$, also being the control design variables. For the dynamic dissipative controller, the closed-loop system matrices in Eq. (13) are

$$\bar{A} = \begin{bmatrix} A & -BC_c \\ B_cC_r & A_c \end{bmatrix}; \quad \bar{H} = \begin{bmatrix} H \\ 0 \end{bmatrix}; \quad \bar{C} = \begin{bmatrix} C_{\text{per}} & 0 \end{bmatrix}$$
 (23)

For average control power computation, $\bar{C}_u = -[0 \quad C_c]^T$. Again, Eqs. (15) and (16) are used for computing control power and rms line-of-sight pointing error. Thus, the scalar variables α_i , β_i , where $i=1,2,\ldots,6$, and q_j , where $j=1,2,\ldots,12$, constitute 24 control design variables. Along with 21 structural design variables, the total number of design variables for integrated redesign with dynamic dissipative controllers is 45.

Table 1 shows the results of designs with the dynamic dissipative controller. The control-optimized design for phase-0 CEM required a control power of 6.41 lb² to maintain rms line-of-sight pointing within 2.4 in. The integrated redesign reduces the average control power by 44% over the conventional design to 3.64 lb². The effective areas for the structural elements for integrated design with the dynamic dissipative compensator are shown in Table 2. Effective areas for longerons, battens, and diagonals for the integrated design with dynamic dissipative controllers show the same trends as those for the static dissipative controller. Control design variables for the control-optimized design variables and the integrated design shown in Table 4. Figure 5 compares the maximum and minimum singularvalue plots of optimal dynamic dissipative controllers for phase-0 CEM (dashed lines) and redesigned system (solid lines). It is observed that the controller gains are generally smaller throughout the frequency spectrum except in the very low-frequency region.

The results obtained for both the static and dynamic dissipative controllers clearly show that integrated controls-structures design

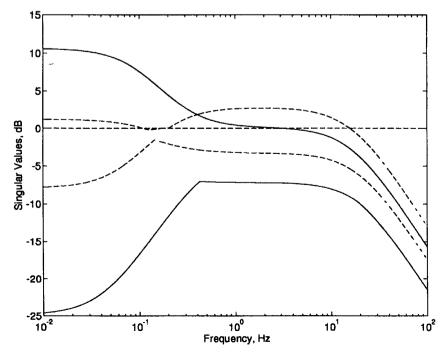


Fig. 5 Maximum and minimum singular-value plots of dynamic dissipative controllers for phase-0 CEM (dashed line) and phase-1 CEM (solid line).

Table 4 Control design variables for integrated design, with dynamic dissipative controllers

Var. no.	Control- optimized design	Integrated design	Var. no.	Control- optimized design	Integrated design
$A_{c[2,1]}$	136.57	135.39	$Q_{[1,1]}$	15,287.63	18,122.76
$A_{c[2,2]}$	105.25	114.73	$Q_{[2,2]}$	30,050.42	12,173.74
$A_{c[4,3]}$	136.60	301.81	$Q_{[3,3]}$	15,125.39	10,430.10
$A_{c[4,4]}$	104.33	102.17	$Q_{[4,4]}$	29,103.43	13,600.71
$A_{c[6,5]}$	103.80	80.42	$Q_{[5,5]}$	19,640.50	24,674.52
$A_{c[6,6]}$	107.72	125.07	$Q_{[6,6]}$	24,331.62	19,487.68
$A_{c[8,7]}$	94.56	58.21	$Q_{[7,7]}$	20,582.68	22,964.97
$A_{c[8,8]}$	121.26	103.52	$Q_{[8,8]}$	22,159.79	21,224.58
$A_{c[10,9]}$	136.92	95.28	$Q_{[9,9]}$	15,148.89	22,693.96
$A_{c[10,10]}$	103.87	107.26	$Q_{[10,10]}$	29,362.52	20,381.06
$A_{c[12,11]}$	100.11	136.11	$Q_{[11,11]}$	20,009.49	17,783.45
$A_{c[12,12]}$	126.11	133.30	$Q_{[12,12]}$	21,511.89	15,376.09

methodology can yield a substantially superior overall design over the conventional sequential design scenario. Moreover, Table 2 shows that the optimal structure for both dissipative control laws exhibit similar trends. In fact, the structural design variables for the two optimal structures are within 20% of each other. A structural design close to both these designs was chosen for fabrication and assembly in the laboratory. This redesigned structure was referred to as phase-1 CEM. A number of active control experiments were performed with both phase-0 and phase-1 CEM to validate the benefits of integrated controls-structures design demonstrated analytically in this paper. This experimental validation is described in Ref. 16.

Concluding Remarks

An optimization-based integrated controls-structures design methodology has been presented in this paper, using static and dynamic dissipative compensators. To demonstrate the benefits of this design approach, the nominal phase-0 CEM structure was redesigned, using the integrated design methodology, to minimize the average control power required to maintain specified rms lineof-sight pointing error under persistent disturbances. The redesign with static dissipative compensators resulted in a 40% reduction in control power, whereas the redesign with dynamic dissipative compensators produced a 44% reduction in control power. Therefore, it has been demonstrated, analytically, that integrated controlsstructures design can yield designs that are substantially superior to those obtained through the traditional sequential approach. Moreover, to show that the benefits achieved analytically can be realized in practice, the redesigned structure was fabricated and assembled in the laboratory. Experimental validation of these results has been performed successfully and is presented in Ref. 16. Finally, this work demonstrates the capability of a software design tool (CSI-DESIGN) that implements the automated design procedure in a unified environment for structural and control designs.

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